Prior Knowledge About Camera Motion for Outlier Removal in Feature Matching

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Abstract: The search of corresponding points in between images of the same scene is a well known problem in many computer vision applications. In particular most structure from motion techniques depend heavily on the correct estimation of corresponding image points. Most commonly used approaches make neither assumptions about the 3D scene nor about the relative positions of the cameras and model both as completely unknown. This general model results in a brute force comparison of all keypoints in one image to all points in all other images. In reality this model is often far too general because coarse prior knowledge about the cameras is often available. For example, several imaging systems are equipped with positioning devices which deliver pose information of the camera. Such information can be used to constrain the subsequent point matching not only to reduce the computational load, but also to increase the accuracy of path estimation and 3D reconstruction. This study presents Guided Matching as a new matching algorithm towards this direction. The proposed algorithm outperforms brute force matching in speed as well as number and accuracy of correspondences, given well estimated priors.

1 INTRODUCTION

Many computer vision algorithms depend on a successful estimation of point correspondences between several images. One example, which is of particular interest for the work discussed here, are Structure from Motion (SfM) techniques that estimate camera positions as well as a 3D model of the scene from a given set of input images. The estimation of point correspondences is a crucial part of such methods, as they rely on them to estimate the underlying geometry of the image set. Although modern approaches successfully showed their potential on many datasets, the point matching procedure still faces many challenges such as ambiguities (e.g. due to repetitive scene patterns), memory consumption, as well as a high computational load.

A commonly used point matching technique is the so-called brute force matching (BFM), which compares every keypoint of an (source) image with every keypoint within a second (target) image. This involves the comparison of every keypoint descriptor of the first image to all keypoint descriptors of the second one. The point-pairs with the smallest difference are kept as matching candidates, which are further processed by several filtering steps. There are many attempts to lift the computational burden of BFM, e.g. by using suitable data structures (e.g. trees (Muja and Lowe, 2012)) or special hardware (e.g. multi-core systems or GPUs (Garcia et al., 2008)). BFM only assumes that the images have a certain pairwise overlap, but makes no further assumptions about the pose of the cameras or point distribution. These basic assumptions make BFM on the one hand easy to implement and generally applicable, but are on the other hand also the main factor for its limitations with respect to speed and accuracy.

(a) One keypoint of the source image
(b) Respective search region in target image

Figure 1: Keypoint and its corresponding search area.
The basic insight of the proposed method is to use available prior knowledge of camera position and orientation to guide the matching procedure by restricting the correspondence search to a specific area within the target image. The right side of Figure 1 shows an example of such a search area that was computed by the Guided Matching (GM) method as proposed by this paper. Only keypoints within this area are used for comparisons while the rest of the points are not taken into consideration. Consequently, fewer comparisons have to be performed and the risk of matching two non-homologous keypoints decreases. Thus, post-processing techniques like point filtering can be avoided. Guided Matcher is especially applicable in cases where texture ambiguities are present.

Geometric constraints in image matching can be imposed in various ways like object scene information, point distribution or camera path constraints etc. This study focuses on the use of easy to acquire path-based constraints, such as noisy location and orientation data in order to achieve efficient outlier removal. Camera positions and orientations are seldom known accurately enough for an automatic 3D reconstruction and thus need to be estimated from the image sequence. However, modelling this sequence as a completely unordered set of images is far too general in a variety of practical scenarios. Nowadays, several camera setups are equipped with systems such as Global Positioning System (GPS) and/or Inertial Navigation System (INS). Unmanned Aerial Vehicles (UAVs), rovers, or even mobile phone cameras (e.g. geotagging) are just a few examples of imaging systems which attach basic location information to their image data. Even in cases where this information is not directly delivered by the imaging system itself, the user might be able to provide a coarse description of the camera setup, e.g. a rough estimation of the path followed during capturing the images.

Although such prior information is often available, it is mostly ignored by current systems. This paper proposes a simple, yet efficient, robust, and accurate method to exploit any prior knowledge about camera location and orientation in a probabilistic manner. If no prior knowledge is available or the uncertainty of the provided information is too large, the system behaviour saturates to that of the standard BFM. In all other cases it leads to superior results with respect to computation time, number of matches, as well as accuracy of the finally estimated epipolar geometry. An overview of the related work is presented in the next section (Section 2). Section 3 describes in detail the proposed method (Guided Matcher, GM), followed by experimental results (Section 4) and conclusions (Section 5).

2 RELATED WORK

During the last years various works have been published towards accurate and efficient keypoint matching with the application to path estimation and 3D reconstruction. State of the art algorithms not only estimate the camera path but also create textured 3D point clouds. Most of them completely exclude any kind of prior information and model the image sequences as an unordered set of images. In 2006 Photo Explorer, a 3D photo browsing interface, was presented (Snively et al., 2006). Their approach uses random pictures of the same object collected from the internet. SIFT (Lowe, 2004) is used for keypoint extraction and description. Camera parameters are recovered through standard SfM techniques. A 3D scene is rendered in order to enable navigation and exploration. A few years later the authors of (Agarwal et al., 2011) made a significant improvement towards handling very large datasets by using parallel computing. Following the typical procedure, coarse SIFT features are extracted, described, and matched. SfM is solved with bundle adjustment. The final output is a sparse 3D model. (Furukawa and Ponce, 2010) further extend the existing multi-view methods and use them to create dense point clouds through a new image clustering algorithm. Their system is able to deal efficiently with very large unorganized photo collections. Other studies use content-based filtering algorithms for unstructured data stored in the Web in order to reconstruct objects of interest (Makantasis et al., 2014).

On the other hand, there are studies that restrict the correspondence search area by using geometric or algebraic constraints. The work of (Baltasavias, 1991) assumes that the cameras are calibrated and have known exterior orientation. Collinearity conditions are used to restrict the search area to a 1D space. In (Hess-Flores et al., 2012) the camera path is projected onto a plane to track image features for aerial video sequences. They use consensus information about the camera parallax to avoid outliers. The approach of (Strelov, 2004) models inertial measurements of the robots motion. In (Wendel, 2013) the geometric prior knowledge about the 3D structure of the scene is modelled for navigation purposes. In (Szeliski and Torr, 1998) keypoint coplanarity is assumed for accurate SfM. In (Lopez, 2013) algebraic epipolar constraints are used to minimize the algebraic epipolar cost between each stereo pair.

In practice it is unlikely that the true epipolar geometry of two images is estimated. Inaccurate keypoint locations, mismatches, and critical keypoint configurations lead to small errors within the final estima-
tion. Consequently, many approaches model the fundamental matrix $F$ as stochastic variable. The uncertainty of $F$ is represented by a covariance matrix $C_F$.

The so-called probabilistic epipolar geometry exploits the knowledge of $C_F$ to improve image matching, projective reconstruction, and self calibration. One example is (Brandt, 2008), which calculates a probability density function of the location of feasible keypoints in the target image. The corresponding point lies in the neighborhood of the narrowest point of the epipolar envelope, e.g., the region defined by all possible epipolar lines. In (Unger and Stojanovic, 2010) point correspondences are evaluated by taking the uncertainty of the epipolar geometry into account.

The above mentioned studies are related to the proposed approach as all of them aim to eliminate false matches during point correspondence search. GM, however, uses more general probabilistic models to describe available prior knowledge and provides a simpler and more efficient scheme to exploit this information for keypoint matching. In cases where no prior knowledge is available, the proposed method is still applicable and simply degenerates to the standard BFM.

3 GUIDED MATCHER

This article studies the potential of using prior knowledge about the location and orientation of the cameras during the search for corresponding keypoints. In practice this prior information is available in many forms, ranging from GPS/INS measurements of UAVs, to GPS tags of modern consumer cameras, to a coarse path description by the user. The only requirement of the proposed method is, that this prior knowledge can be expressed as probability density function of location $p(t)$ and pose $p(R)$ for each camera $c$.

A simple example is that both quantities are Gaussian distributed $p(t) \sim N(\mu_c, \Sigma_c)$, $p(R) \sim N(\mu_c, \Sigma_c)$, where the mean values $\mu_c, \Sigma_c$ of $\gamma_1, \gamma_2$ as well as the variance-covariance matrices $\Sigma_c \in \mathbb{R}^{6 \times 6}$ represent the given prior knowledge.

The proposed framework can be applied to the matching of any kind of image quantities, including points, lines, and planes. For the sake of simplicity the following discussion is restricted to the standard case of matching keypoints. These have to be detected and described before the matching procedure by any of the available keypoint detectors/descriptors such as SIFT, SURF, FAST, etc. (see for example Mikolajczyk and Schmid, 2004; Mikolajczyk and Schmid, 2005 for more details on keypoint detection/description).

Given a pair of cameras $c_1,c_2$ as well as their respective calibration matrices $K_1,K_2$, their corresponding lists of keypoints, and the probability densities $p_c(R), p_c(t), p_{c_1}(t), p_{c_2}(t)$ describing the prior distribution of location and orientation, the proposed method (as summarized by Algorithm 1) restricts the search area for each point of the source image instead of comparing it to all possible points in the target image. The following explanation only briefly mentions established concepts of epipolar geometry. More extensive as well as more detailed information about stereo vision can be found in (Hartley and Zisserman, 2003).

**Algorithm 1: Guided Matching.**

Require: Set of keypoints $K_{P_i}$, Calibration $K_i$, Prior knowledge $p_i(R), p_i(t)$ ($i \in \{1, 2\}$)

Sample $N$ different $R_i$ and $t_i$ from $p_i(R)$ and $p_i(t)$

Compute $F^i$ from $(t_{12}^i, R_{12}^i, K_1)$ and $(t_{12}^i, R_{12}^i, K_2)$

for every keypoint $k_{P_1} \in K_{P_1}$ do

define search area based on set of fundamental matrices $F^i$

for every keypoint $k_{P_2} \in K_{P_2}$ do

if $k_{P_2}$ is inside search area then

compute distance between $k_{P_1}$ and $k_{P_2}$

end if

end for

keep $k_{P_2}$ with minimal distance as corresponding point to $k_{P_1}$

end for

Several rotation matrices $R_i^j$ and location vectors $t_i^j$ ($i \in \{1, 2\}, j = 1,...,N$) are sampled for each camera $c_i$ from the provided probability densities and combined to a roto-translation matrix $Q_i^j$ by Equation 1.

$$Q_i^j = \begin{bmatrix} R_i^j & t_i^j \\ 0 & 1 \end{bmatrix}$$

The relative roto-translation matrix $Q_{12}^j$ from camera $c_1$ to camera $c_2$ is then given by Equation 2.

$$Q_{12}^j = (Q_1^j)^{-1} \cdot Q_2^j = \begin{bmatrix} R_{12}^j & t_{12}^j \\ 0 & 1 \end{bmatrix}$$

where $R_{12}^j$ and $t_{12}^j$ are the relative rotation and translation from camera $c_1$ and $c_2$.

The fundamental matrix describing this geometric setup can then be calculated by Equation 3.

$$F^j = K_{12}^T R_{12}^j \begin{bmatrix} t_{12}^j \end{bmatrix} K_1$$

where $K_i$ are the calibration matrices of the cameras and $t_{12}^j$ is the skew-symmetric matrix-representation of vector $t_{12}^j$. 

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The search region of each of the keypoints of the source image is constructed as follows: For a given point \( x_1 \) in the source image each of the \( N \) different fundamental matrices leads to one epipolar line \( l_2 = F_j \cdot x_1 \) in the target image (Figure 2(a)). The convex envelope of all these lines is approximated by the extreme intersections of these lines with the image borders as well as a vertical line in the image center.

Potential correspondences of a point are assumed to lie only inside this area. Every keypoint of the target image is tested whether it is inside the estimated polygon (Figure 2(b)). Only if this is the case the far more expensive calculation of the (Euclidean) distance between both keypoint descriptors is carried out. The point with the smallest distance is kept as corresponding point (Figure 2(c)).

Thus, instead of doing an exhaustive search, i.e. comparing each keypoint of the source image with every keypoint of the target image, it is compared with a significantly smaller subset of keypoints. On the one hand, the number of necessary comparisons is limited which leads to a substantial decrease of the computational load. On the other hand, it increases the probability of finding a correct match. BFM defines the global best match as corresponding point. GM excludes huge portions of an image, that might contain similar areas in terms of geometry or radiometry. These areas lead to wrong correspondences if BFM methods are used (Figure 2(d)). It should be noted that GM is not able to resolve all ambiguities. If the best global (but wrong) match lies outside the search area, GM is more likely to give the correct point correspondence. However, if the best global (but wrong) match lies inside the borders of the area it will be defined as corresponding point by both methods.

The distribution of the epipolar lines and consequently the shape of the computed envelope depends on the accuracy of the prior knowledge. The more accurate the priors are, the narrower the envelope is as shown exemplary in Figure 3. In the extreme case that the prior knowledge exactly models the true position and orientation of the cameras, the envelope reduces to the true epipolar line. In the other extreme case the uncertainty of the prior information is too large, the search area approaches the area of the whole image, and GM behaves almost identically to BFM.
4 EXPERIMENTS

The following experiments are designed to evaluate the performance of the proposed matching algorithm (GM) and compare it to the standard brute force matching (BFM) approach. Both methods are applied to all adjacent image pairs of the Castle-P19, Castle-P30, Entry-P10, Fountain-P11, Herz-Jesu-P8, and Herz-Jesu-P25 image data sets (Strecha et al., 2008), which provide reference data of the absolute camera poses additionally to the images. In total nearly 100 image pairs were processed. The results presented below are averaged over all these image pairs and depict the performance of GM relative to BFM. That means in particular, that the absolute performances of GM \( P_{GM} \) and BFM \( P_{BFM} \) are combined to the relative performance \( P \) by Equation 4, where \( P \) stands for any of the following measurements which are displayed in Figures 4-7.

\[
P = \frac{P_{GM}}{P_{BFM}}
\]  

(a) Ratio of number of matches  
(b) Ratio of mean Sampson error with respect to true fundamental matrix (all matches)

Figure 4: Relative performance of GM and BFM (see Eq. 4).

SURF, used as keypoint detector/descriptor for its computational speed and robustness, detected between 3200 and 9200 keypoints (around 5500 on average). The prior knowledge is modelled as Gaussian distributions \( p_c(R) \sim N(\mu_{R}, \Sigma_{R}) \), \( p_c(t) \sim N(\mu_{t}, \Sigma_{t}) \), where the mean values \( \mu_{R}, \mu_{t} \) are based on the provided reference data. The variance-covariance matrices \( \Sigma_{R}, \Sigma_{t} \) are modelled as diagonal matrices with identical entries \( \sigma_{R}^2 = \sigma_{t}^2 = \sigma^2 \) on the main diagonal. This model is seldom true in practice since often at least one of the directions is known with higher certainty than the others (e.g. in the case of planar movement). However, it restricts the amount of variables and allows an easy visualization while still capturing the main properties of the proposed algorithm. From the given probability density function 100 different locations and orientations are sampled for each camera, which are subsequently combined to 100 fundamental matrices as described above (see Equation 3). All the figures below have common logarithmic axes depicting \( \sigma_{R}^2 \) in degree and \( \sigma_{t}^2 \) in meter.

Figure 4(a) shows the ratio of the number of matches found by both methods. While BFM always returns a match, GM might not if the established search area of a keypoint does not contain any points. The probability of this case increases with lower uncertainty values, which leads to a ratio smaller than one. However, even for very narrow search regions more than 90% of the number of matches of BFM are found. It should be noted, that even if both methods return the same number of matches, they probably will not be the same matches (see discussion below).

Usually the established set of corresponding points is filtered before it is used to estimate the fundamental matrix. However, it is interesting to see that even the unfiltered set of matches can already lead to reasonable results for GM. Figure 4(b) depicts the ratio of the mean Sampson error of both methods if the matched keypoints are compared to the fundamental matrix which is computed from the provided reference data. For a small amount of uncertainty the Sampson error of the GM matches approaches zero, while it is still reasonable small for a medium amount of uncertainty.

(a) Ratio of RANSAC inliers  
(b) Ratio of numbers of filtered matches

Figure 5: Relative performance of GM and BFM (see Eq. 4).

If RANSAC is used to estimate the fundamental matrix based on the found matches, the number of inliers gives a good cue about the correctness of the correspondence of the point sets. Figure 5(a) shows the ratio of inliers of both methods. It should be noted, that the absolute number of inliers is used. GM results always in a greater or equal number of inliers (up to a factor of six more), even if less matches (e.g. only 95%) are available.

Although beyond the scope of this paper, a simple and well known filtering method is applied to the found matches: A match is kept iff the ratio of the
distances between the best and the second best match exceeds a certain threshold. Figure 5(b) shows the ratio of the number of matches that remained after this ratio filter. Similar to the discussion above the absolute numbers are used to compute the ratio. Nevertheless, GM results always in a larger or equal number of filtered matches than BFM.

Figure 6 shows the ratio of RANSAC inliers and the mean Sampson error with respect to the true fundamental matrix if the filtered matches are used instead of all matches. Again GM outperforms BFM if the uncertainty of the prior knowledge is small enough and leads to identical results otherwise. The absolute mean Sampson error of both methods is significantly reduced by using filtered matches.

It should be noted that, although the mean Sampson error of GM is always smaller or equal to the error of GM (Figure 6(b)), this does not necessarily hold for the maximal Sampson error as Figure 7(a) shows. Lets assume the search area as a horizontal band. Any keypoint in the image which is similar with respect to its descriptor will be found by BFM. If this best (but wrong) match shows a vertical displacement, it will not be considered by GM, because it is outside of the search area. GM searches for the best match inside the search area, which might be located at the other side of the image and thus showing a much larger spatial distance allowing for a larger Sampson error.

Figure 6: Relative performance of GM and BFM (see Eq. 4).

All of the above discussion is concerned with the relative accuracy of GM and BFM with respect to quantitative as well as qualitative measurements. Figure 7(b) depicts the ratio of computation time, that was needed on average in order to compute the point correspondences. As long as the prior knowledge is given with a sufficient amount of certainty GM is significantly faster than BFM. But for too high uncertainty the search regions span the most part of the image, which results in a saturation of the accuracy of GM to the performance of BFM. In this case the same comparisons are carried out by both methods, leading to identical results. The overhead to compute the search regions, however, leads to a further increase of computational time.

Figure 7: Relative performance of GM and BFM (see Eq. 4).

The range of uncertainty of the prior knowledge where GM shows its full potential occurs to be rather small within the above experiments. However, it should be noted, that the uncertainty is given with respect to the absolute camera position and orientation. The fundamental matrix depicts the relative orientation of the two cameras and consequently is basically given with twice the amount of uncertainty as the absolute positions. In applications where the relative position is given as prior knowledge (e.g. by motion models or inertial measurements) the range of values where GM leads to reasonable increase of performance can be doubled. Furthermore, often at least one of the possible moving or looking directions is given with much higher accuracy, e.g. in the case of planar motion where the height component of the translation as well as the variation of the pitch angles are negligible.

5 CONCLUSIONS

Prior knowledge about the position and orientation of the cameras is available in many practical scenarios: UAVs often fly a path given by predefined GPS locations, modern consumer cameras attach GPS tags to their image data, mobile phones have access to GPS data as well and can provide additional measurements of the relative movement, and last but not least, the user, who acquired the image data, might be able to give a coarse description of the path he took during data acquisition. Nevertheless, most modern methods
of keypoint matching disregard this knowledge completely and assume the most general case in which no prior knowledge is available whatsoever.

The goal of this paper is to propose a simple, efficient, and accurate method to include this prior knowledge into the task of keypoint matching. Camera positions and orientations are modelled as probability density distributions from which several fixed poses are sampled. These are combined to a set of possible fundamental matrices. For each keypoint of the first image each of these matrices defines one epipolar line in the other image. An approximation of the convex envelope of these epipolar lines defines the area in which the matching keypoint is searched. Keypoints outside this area are not considered and do not need to be compared to the source keypoint. If the search areas are sufficiently small (i.e. the prior knowledge sufficiently accurate) this approach saves computation time since considerably less comparisons have to be carried out. Additionally, the correspondence set will be much more accurate since problems due to repetitive image structures can be resolved more easily leading to less ambiguous matches.

The results of the experimental section show that these theoretical considerations are valid. GM leads to superior performance with respect to quantitative (e.g. number of valid matches) as well as qualitative (e.g. mean Sampson error) measurements, while being also significantly faster than BFM. If the uncertainty of the prior knowledge is too large, the performance of GM saturates to BFM leading to identical matches.

It should be noted that all optimization techniques that are usually applied to enhance BFM methods can equally be applied to GM. All keypoints are handled independently which allows for parallel processing.

Future work will focus on a more efficient definition of search regions to reduce the overhead on calculations. Also an easy to use but general graphical user interface will be developed to allow the user to provide the available prior knowledge in any given form. Last but not least the method presented in this paper should be extended by including other types of prior knowledge, e.g. about the 3D scene structure, to further enhance results.

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